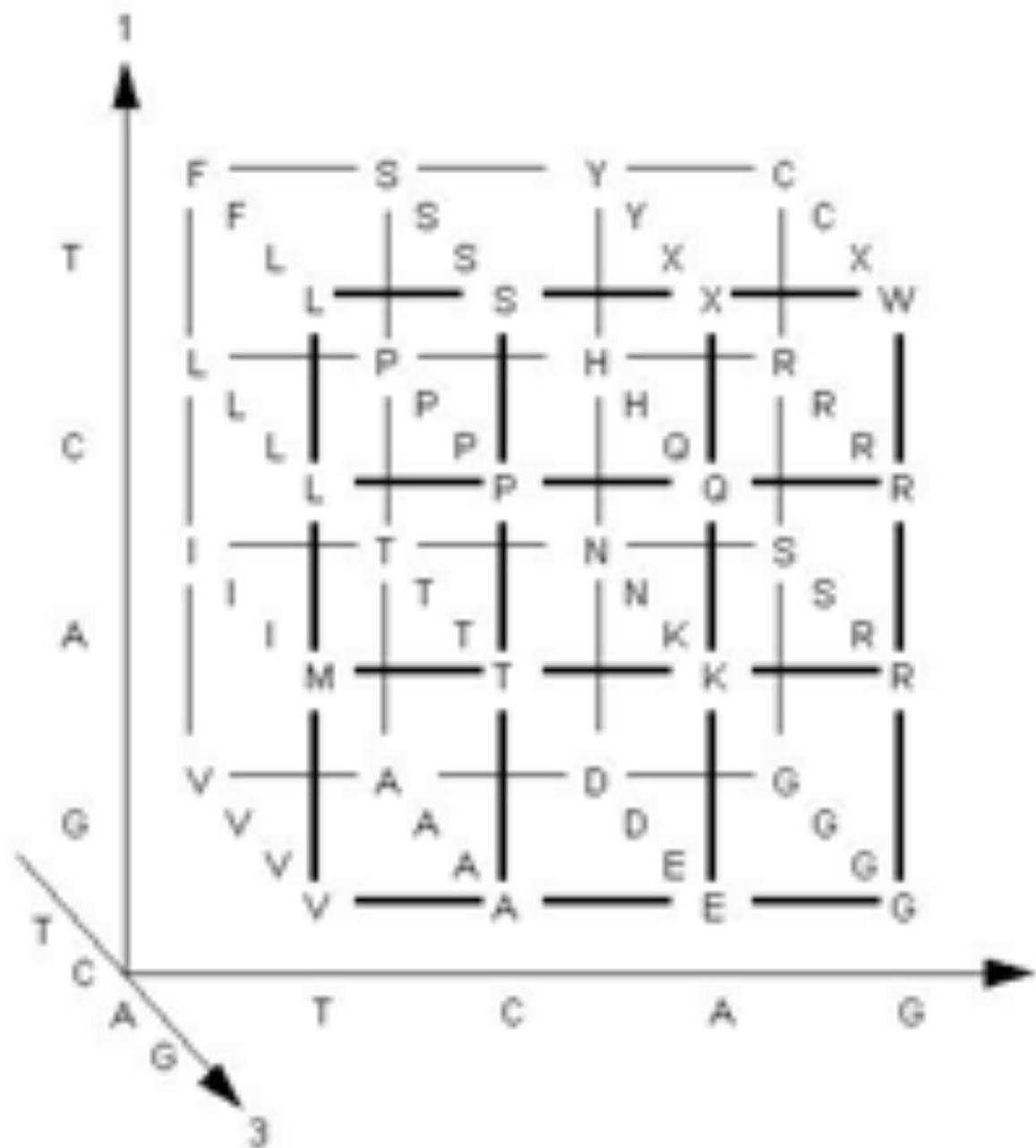


(\* Genetic code



\*)

(\* 64 {a,c,g,t} codons in binary in a,c,g,t order as defined by the following \*)

```

t=.; g=.; c=.; a=.;
nucgc = Tuples[{a, c, g, t}, 3];
a = {1, 0, 0, 0};
c = {0, 1, 0, 0};
g = {0, 0, 1, 0};
t = {0, 0, 0, 1};

nucgc = Flatten[nucgc];
nucgc = Partition[nucgc, 12];

pivns = PseudoInverse[nucgc]; (*corrected*)

(*
codon triplets entered manually in canonical order by alphabet -
as above in matrix

AAA
AAC
AAG
AAT
ACA
ACC
ACG
ACT
AGA
AGC
AGG
AGT
ATA
ATC
ATG
ATT
CAA
CAC
CAG
CAT
CCA
CCC
CCG
CCT
CGA
CGC
CGG
CGT
CTA
CTC

```

CTG  
CTT  
GAA  
GAC  
GAG  
GAT  
GCA  
GCC  
GCG  
GCT  
GGA  
GGC  
GGG  
GGT  
GTA  
GTC  
GTG  
GTT  
TAA  
TAC  
TAG  
TAT  
TCA  
TCC  
TCG  
TCT  
TGA  
TGC  
TGG  
TGT  
TTA  
TTC  
TTG  
TTT

manually copy the triplets from above and replace  
with amino acid single letter code, in identical order,  
and make matrix 'aagc' for amino acid genetic code, including 3 stop codons

\*)

```
(* Map an attribute of the amino acids onto the triplet codons *)  
  
jjt =.  
  
a =.;  
c =.;  
d =.;  
e =.;  
f =.;  
g =.;  
h =.;  
i =.;  
k =.;  
l =.;  
m =.;  
n =.;  
p =.;  
q =.;  
r =.;  
s =.;  
t =.;  
v =.;  
w =.;  
x =.; y =.;  
  
jjt = {{k}, {n}, {k}, {n}, {t}, {t}, {t}, {t}, {r}, {s}, {r}, {s}, {i}, {i}, {m}, {i},  
{q}, {h}, {q}, {h}, {p}, {p}, {p}, {p}, {r}, {r}, {r}, {r}, {r}, {l}, {l}, {l}, {l},  
{e}, {d}, {e}, {d}, {a}, {a}, {a}, {a}, {g}, {g}, {g}, {g}, {v}, {v}, {v}, {v},  
{x}, {y}, {x}, {y}, {s}, {s}, {s}, {s}, {x}, {c}, {w}, {c}, {l}, {f}, {l}, {f}};  
  
nuchyd =.;  
  
nuchyd = pivns.jjt;
```

```

(* 20 K&D hydropathy values, padded with 0.0 for stop *)
(* checked against http://
web.expasy.org/protscale/pscale/Hphob.Doolittle.html *)

kd = {1.8, 2.5, -3.5001, -3.5002, 2.8, -0.4, -3.2, 4.5, -3.9, 3.8, 1.9,
      -3.5003, -1.6, -3.5004, -4.5, -0.8, -0.7, 4.2, -0.9, 0.0, -1.3};

a = kd[[1]];
c = kd[[2]];
d = kd[[3]];
e = kd[[4]];
f = kd[[5]];
g = kd[[6]];
h = kd[[7]];
i = kd[[8]];
k = kd[[9]];
l = kd[[10]];
m = kd[[11]];
n = kd[[12]];
p = kd[[13]];
q = kd[[14]];
r = kd[[15]];
s = kd[[16]];
t = kd[[17]];
v = kd[[18]];
w = kd[[19]];
x = kd[[20]];
y = kd[[21]];

nuchyd (* numeric with above hydropathy values *)

{{-0.638625}, {-1.25125}, {0.68625}, {0.880375}, {-2.63938}, {-0.163375},
 {-1.46963}, {3.94913}, {-0.169937}, {0.117688}, {-0.388687}, {0.117688}},

(* Reconstruct hydropathy values from nucleotide information
using dot product of a weighted vector for triplets *)
(* use single letter code for new vectors, precede by the letter 'a',
because variables are global *)

(* Watch out! Triplets are in A,C,G,T for use here *)

aa = {0, 0, 1, 0, 0, 1, 0, 0, .25, .25, .25, .25};
aanuc = Total[aa.nuchyd, 2]

ac = {0, 0, 0, 1, 0, 0, 1, 0, 0, 0.5, 0, 0.5};

```

```

acnuc = Total[ac.nuchyd, 2]

ad = {0, 0, 1, 0, 1, 0, 0, 0, 0, 0.5, 0.0, 0.5};
adnuc = Total[ad.nuchyd, 2]

ae = {0, 0, 1, 0, 1, 0, 0, 0, 0.5, 0, 0.5, 0};
aenuc = Total[ae.nuchyd, 2]

af = {0, 0, 0, 1, 0, 0, 0, 1, 0, 1, 0, 1};
afnuc = Total[af.nuchyd, 2]

ag = {0, 0, 1, 0, 0, 0, 1, 0, .25, .25, .25, .25};
agnuc = Total[ag.nuchyd, 2]

ah = {0, 1, 0, 0, 1, 0, 0, 0, 0, 0.5, 0, 0.5};
ahnuc = Total[ah.nuchyd, 2]

ai = {1, 0, 0, 0, 0, 0, 0, 1, 1/3, 1/3, 0, 1/3};
ainuc = Total[ai.nuchyd, 2]

ak = {1, 0, 0, 0, 1, 0, 0, 0, 0.5, 0, 0.5, 0};
aknuc = Total[ak.nuchyd, 2]

al = {0, 2/3, 0, 1/3, 0, 0, 0, 1, 2/6, 1/6, 2/6, 1/6};
alnuc = Total[al.nuchyd, 2]

am = {1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0};
amnuc = Total[am.nuchyd, 2]

an = {1, 0, 0, 0, 1, 0, 0, 0, 0, 0.5, 0, 0.5};
annuc = Total[an.nuchyd, 2]

ap = {0, 1, 0, 0, 0, 1, 0, 0, .25, .25, .25, .25};
apnuc = Total[ap.nuchyd, 2]

aq = {0, 1, 0, 0, 1, 0, 0, 0, 0.5, 0, 0.5, 0};
aqnuc = Total[aq.nuchyd, 2]

ar = {1/3, 2/3, 0, 0, 0, 0, 0, 1, 0, 1/3, 1/6, 1/3, 1/6};
arnuc = Total[ar.nuchyd, 2]

as = {1/3, 0, 0, 2/3, 0, 2/3, 1/3, 0, 1/6, 1/3, 1/6, 1/3};
asnuc = Total[as.nuchyd, 2]

at = {1, 0, 0, 0, 0, 1, 0, 0, .25, .25, .25, .25};
atnuc = Total[at.nuchyd, 2]

av = {0, 0, 1, 0, 0, 0, 0, 1, .25, .25, .25, .25};
avnuc = Total[av.nuchyd, 2]

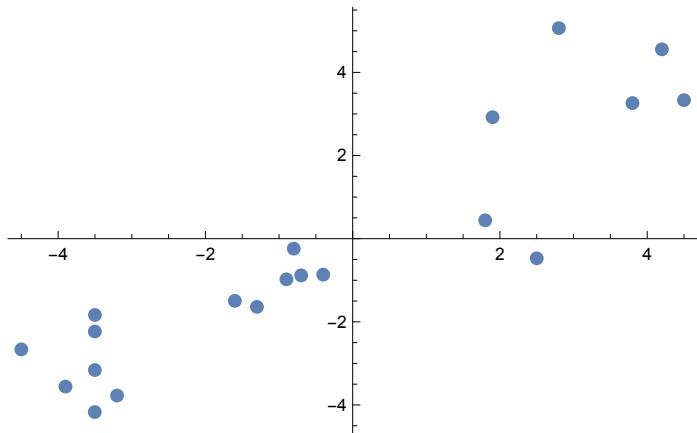
```

```
aw = {0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 1, 0};  
awnuc = Total[aw.nuchyd, 2]  
  
ax = {0, 0, 0, 1, 2/3, 0, 1/3, 0, 2/3, 0, 1/3, 0};  
axnuc = Total[ax.nuchyd, 2]  
  
ay = {0, 0, 0, 1, 1, 0, 0, 0, 1/2, 0, 1/2};  
aynuc = Total[ay.nuchyd, 2]  
0.442063  
-0.471563  
-1.83544  
-2.23244  
5.06488  
-0.864187  
-3.77294  
3.33231  
-3.55731  
3.26144  
2.92181  
-3.16031  
-1.49544  
-4.16994  
-2.66365  
-0.239396  
-0.882813  
4.55456  
-0.977938  
-1.61194  
-1.64131
```

```
(* Fill empirical and SVP values for hydropathy into a 20 x 2 matrix *)

paired = {{a, aanuc}, {c, acnuc}, {d, adnuc}, {e, aenuc},
  {f, afnuc}, {g, agnuc}, {h, ahnuc}, {i, ainuc}, {k, aknuc},
  {l, alnuc}, {m, amnuc}, {n, annuc}, {p, apnuc}, {q, aqnuc}, {r, arnuc},
  {s, asnuc}, {t, atnuc}, {v, avnuc}, {w, awnuc}, {y, aynuc}};

ListPlot[paired, PlotStyle -> PointSize[0.02]]
FindFit[paired, intercept + slope * xaxis, {intercept, slope}, xaxis]
Correlation[Take[paired, All, {1}], Take[paired, All, {2}]]
```



```
{intercept → 0.00335099, slope → 0.862013}
```

```
 {{0.914202}}}
```

(\*  
Reaction Centers of Photosynthetic Bacteria (1990) Michel-Beyerle M.ed. pp.209-218,  
Springer-Verlag Berlin. Genetic Coding Algorithms for  
Engineering Membrane Proteins. Yang M.M., Coleman, W.J., & Youvan,  
D.C. Massachusetts Institute of Technology, Department of Chemistry,  
Cambridge 02139. Abstract available at  
<http://www.kairos-scientific.com/searchable/abstracts/Yang1990.htm> and quoted here:

A solution to the problem of relating the physicochemical properties of the amino acids to their codon sequences has been achieved by treating the genetic code as a system of linear equations and applying the numerical method, Singular Value Decomposition (SVD). For example, hydropathy and molar volume, which are important determinants of protein structure and function, can be quantitatively related to the nucleotide sequence. The 20 hydropathy values of the amino acid residues were remapped to 12 nucleotide-determined values which, in turn, were used to predict structural aspects the photosynthetic reaction center protein, without DNA→protein translation.

\*)

```
(* hotmap *)

hotmap = Table[{
  Piecewise[{{
    {1, 1 <= i < 42},
    {1, 42 <= i < 84},
    {Floor[5.8 * (i - 83)], 84 <= i < 128},
    {256, 128 <= i < 170},
    {256, 170 <= i < 212},
    {256, 212 <= i <= 256}
  }],
  Piecewise[{{
    {1, 1 <= i < 42},
    {(i - 41) * 6, 42 <= i < 84},
    {256, 84 <= i < 128},
    {256 - (i - 128) * 6, 128 <= i < 170},
    {1, 170 <= i < 212},
    {Floor[(i - 211) * 5.7], 212 <= i <= 256}
  }],
  Piecewise[{{
    {Floor[i * 5.8], 1 <= i < 42},
    {256 - ((i - 42) * 6), 42 <= i < 84},
    {1, 84 <= i < 128},
    {1, 128 <= i < 170},
    {((i - 169) * 6, 170 <= i < 212},
    {256, 212 <= i <= 256}
  ]}]
},
{i, 1, 256, 1}];

hotmap[[1, All]] = 1; (* This changes 1,1,
5 to 1,1,1 at i=1 for the blue channel *)

(* Pseudocolor 61 x 12 pivns matrix *)

(* get scaling factors *)

graymat = pivns;
graymin = Min[graymat]
graymax = Max[graymat]
delta = graymax - graymin

-  $\frac{1}{96}$ 

 $\frac{5}{96}$ 

 $\frac{1}{16}$ 
```

```
(* rescale graymat according to min max to get grayscales of 1 to 256 *)

For[x = 1, x ≤ 12, x++,
  For[y = 1, y ≤ 61, y++,
    graymat[[x, y]] = Floor[(graymat[[x, y]] - (graymin)) * (255 / delta) + 1]];
]

colormat = Table[{x, y}, {x, 12}, {y, 61}];
colormat[[All, All]] = {0, 0, 0};
For[x = 1, x ≤ 12, x++,
  For[y = 1, y ≤ 61, y++,
    colormat[[x, y]] = hotmap[[graymat[[x, y]]]] / 256
  ]];
]

gmat = Graphics[RasterArray[Apply[RGBColor, colormat, {2}]],
  ImageSize → {10 * 61, 10 * 12}, AspectRatio → Automatic];
Show[
  gmat]

Part::partw : Part 17387547842683 of
{{1, 1, 1}, {1, 1, 11}, {1, 1, 17}, {1, 1, 23}, {1, 1, 29}, {1, 1, 34}, {1, 1, 40}, {1, 1, 46}, {1, 1, 52}, {1, 1, 58}, {1, 1, 63}, {1, 1, 69}, {1, 1, 75},
{1, 1, 81}, {1, 1, 87}, {1, 1, 92}, {1, 1, 98}, {1, 1, 104}, {1, 1, 110}, {1, 1, 116}, {1, 1, 121}, <<9>>, {1, 1, 179}, {1, 1, 185}, {1, 1, 191},
{1, 1, 197}, {1, 1, 203}, {1, 1, 208}, {1, 1, 214}, {1, 1, 220}, {1, 1, 226}, {1, 1, 232}, {1, 1, 237}, {1, 6, 256}, {1, 12, 250}, {1, 18, 244},
{1, 24, 238}, {1, 30, 232}, {1, 36, 226}, {1, 42, 220}, {1, 48, 214}, {1, 54, 208}, <<206>>} does not exist. >>

Part::partw : Part 17387547842683 of
{{1, 1, 1}, {1, 1, 11}, {1, 1, 17}, {1, 1, 23}, {1, 1, 29}, {1, 1, 34}, {1, 1, 40}, {1, 1, 46}, {1, 1, 52}, {1, 1, 58}, {1, 1, 63}, {1, 1, 69}, {1, 1, 75},
{1, 1, 81}, {1, 1, 87}, {1, 1, 92}, {1, 1, 98}, {1, 1, 104}, {1, 1, 110}, {1, 1, 116}, {1, 1, 121}, <<9>>, {1, 1, 179}, {1, 1, 185}, {1, 1, 191},
{1, 1, 197}, {1, 1, 203}, {1, 1, 208}, {1, 1, 214}, {1, 1, 220}, {1, 1, 226}, {1, 1, 232}, {1, 1, 237}, {1, 6, 256}, {1, 12, 250}, {1, 18, 244},
{1, 24, 238}, {1, 30, 232}, {1, 36, 226}, {1, 42, 220}, {1, 48, 214}, {1, 54, 208}, <<206>>} does not exist. >>

Part::partw : Part 17387547842683 of
{{1, 1, 1}, {1, 1, 11}, {1, 1, 17}, {1, 1, 23}, {1, 1, 29}, {1, 1, 34}, {1, 1, 40}, {1, 1, 46}, {1, 1, 52}, {1, 1, 58}, {1, 1, 63}, {1, 1, 69}, {1, 1, 75},
{1, 1, 81}, {1, 1, 87}, {1, 1, 92}, {1, 1, 98}, {1, 1, 104}, {1, 1, 110}, {1, 1, 116}, {1, 1, 121}, <<9>>, {1, 1, 179}, {1, 1, 185}, {1, 1, 191},
{1, 1, 197}, {1, 1, 203}, {1, 1, 208}, {1, 1, 214}, {1, 1, 220}, {1, 1, 226}, {1, 1, 232}, {1, 1, 237}, {1, 6, 256}, {1, 12, 250}, {1, 18, 244},
{1, 24, 238}, {1, 30, 232}, {1, 36, 226}, {1, 42, 220}, {1, 48, 214}, {1, 54, 208}, <<206>>} does not exist. >>

General::stop : Further output of Part::partw will be suppressed during this calculation. >>

RasterArray::obs : RasterArray is obsolete. Translating to Raster. >>
```

